

Titanium doping effect on the characteristic properties of sol-gel deposited ZnO thin films

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Abstract

Undoped and Ti doped ZnO thin films were made by sol-gel spin coating, and the investigation of structural, morphological and optical features was applied as a function of the doping ratio. The films had a polycrystalline ZnO wurtzite crystal structure with (002) preferential direction and film crystallinity decreased with Ti doping content. The SEM studies indicated that the nanoparticle structure of undoped films changed to nano-network like structure with Ti doping. The transmittance and optical band gap of undoped sample firstly increased with 1 at.% Ti doping and then they decreased with higher Ti level. Consequently, the present work suggests that the characteristic properties of ZnO can be tailored with Ti doping and ZnO:Ti films have a potential importance for usage in many technological applications.

Key words: ZnO, sol-gel preparation, Ti doping, thin films

1. Introduction

Zinc oxide is one of the most studied metal-oxide semiconductors due to its low cost, easy fabrication, non-toxicity, good optical transparency in the visible region and low electrical resistivity [1–3]. These properties make it a good potential candidate for usage in the solar cells, diodes, photodetectors, sensors and liquid crystal displays [4–6]. ZnO is an n-type semiconductor due to the lack of stoichiometry, and the doping of ZnO can allow tailoring the characteristic properties of ZnO. Titanium (Ti), which is one of the doping elements, has 4+ oxidation states and if Ti^{4+} is replaced with Zn^{2+} ions in ZnO lattice, it gives extra free electrons, which causes an increase in electrical conductivity and optical transmittance.

The sol-gel spin coating is a widely used method to prepare ZnO thin film owing to its safety, easy manipulation, simplicity, low cost and easy control of deposition [7]. In the literature, there are a few previous studies on Ti doped ZnO. However, there is no report on sol-gel deposition process of Ti doped ZnO. Therefore, more studies should be conducted on Ti doping

into ZnO, and it is necessary to investigate the Ti doping effect on the features of ZnO. In this study, we have deposited the Ti doped ZnO thin films by sol-gel spin coating, and we have examined the Ti doping effect on the structural, morphological and optical properties of ZnO thin films.

2. Experimental

In this research, undoped and Ti doped ZnO thin films were deposited on glass substrates by spin coating sol-gel method. 1M zinc acetate dehydrate ($\text{Zn}(\text{CH}_3\text{COO})_2 \cdot 2\text{H}_2\text{O}$) and 1M titanium (IV) butoxide ($\text{Ti}(\text{OCH}_2\text{CH}_2\text{CH}_2\text{CH}_3)_4$) were dissolved in 2-Methoxyethanol ($\text{C}_3\text{H}_8\text{O}_2$) solvent, and monoethanolamine ($\text{C}_2\text{H}_7\text{NO}$, MEA) was separately added to this solution as stabilizer. The sol solutions at required quantities were mixed to prepare undoped, and Ti doped ZnO thin films. In the spin coating process, solutions were dropped on glass substrates, which were rotated at a speed of 3000 rpm for 20 s by using a spin-coater and then the films were heated at

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Table 1. Standard and calculated ‘*d*’ values of undoped and Ti doped ZnO thin films

(hkl)	Standard ‘ <i>d</i> ’ (nm)	ZO	TZO-1	TZO-2	TZO-3	TZO-4	TZO-5
		<i>d</i> (nm)	<i>d</i> (nm)	<i>d</i> (nm)	<i>d</i> (nm)	<i>d</i> (nm)	<i>d</i> (nm)
(100)	0.28143	0.27739	0.27698	0.27737	0.27752	0.27771	0.27789
(002)	0.26033	0.25670	0.25655	0.25689	0.25709	0.25721	0.25722
(101)	0.24759	0.24413	0.24408	0.24461	0.24462	0.24497	0.24589
(102)	0.19111	0.18938	–	–	–	–	–
(110)	0.16247	0.16101	0.16142	0.16142	–	–	–
(103)	0.14771	0.14667	0.14650	0.14683	–	–	–

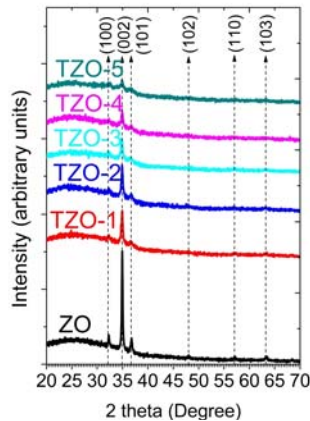


Fig. 1. XRD images of undoped and Ti doped ZnO thin films.

200 °C for 5 min. This procedure was repeated for 5 times and finally, they were annealed in air at 500 °C for 30 min. The undoped and 1, 2, 3, 4, 5 at.% Ti doped films were named to be ZO, TZO-1, TZO-2, TZO-3, TZO-4, TZO-5, respectively. The characterization of films was made by X-ray diffraction (XRD-Rigaku Miniflex II diffractometer), scanning electron microscope (SEM-FEI inspect S50 SEM) and UV-VIS spectrophotometer (Perkin-Elmer, Lambda 40).

3. Results and discussion

3.1. Structural properties

The structural properties of undoped and Ti doped ZnO films were investigated by XRD. The XRD patterns of the samples (Fig. 1) indicate that the films have polycrystalline ZnO hexagonal wurtzite structure (JCPDS card file no. 36-1451) with (002) preferential orientation along *c*-axis. The preferred orientation of (002) was also observed by Liu et al. [8]. The peaks of (100), (101), (102), (110) and (103) are also observed for undoped ZnO. The peaks of (102), (110) and (103) disappear when Ti atoms are inserted into the ZnO structure. The intensities of (100), (002) and

(101) peaks continuously decrease with Ti doping content, which suggests a decrease in the crystallinity of ZnO thin films. The interplanar distance ‘*d*’ values of films are determined by Bragg’s law [9]:

$$n\lambda = 2d \sin \theta, \quad (1)$$

where *n* is one, λ is the wavelength of the incident X-ray beam that is 1.5418 Å, and θ is the diffraction angle. The calculated ‘*d*’ values are presented in Table 1, and these values are compared with the standard value which is taken from the JCPDS card no: 36-1451. The matching standard and calculated ‘*d*’ values also indicate that films have ZnO wurtzite structure. The lattice constants ‘*a*’ and ‘*c*’ of the ZnO wurtzite structure are identified by the relation [10]:

$$\frac{1}{d^2} = \frac{4}{3} \left(\frac{h^2 + k^2 + hk}{a^2} \right) + \left(\frac{l^2}{c^2} \right). \quad (2)$$

The lattice constant values of undoped and Ti doped ZnO thin films are tabulated in Table 2. The lattice constant values are found slightly lower than the standard values of $a_0 = 0.32498$ nm and $c_0 = 0.52066$ nm (JCPDS card no: 36-1451). The lattice constants initially drop off with Ti doping and further Ti doping causes a continuous increment in lattice constant values. This can be resulted from the ionic radii of different oxidation states of titanium. At low doping levels, Ti^{4+} ions are probably replaced by Zn^{2+} ions and this causes a decrease in the lattice constant due to the lower ionic radius of Ti^{4+} (60.5 pm) than one of Zn^{2+} (74 pm) [11]. At high doping levels, Ti^{4+} ions can be reduced to Ti^{3+} (67 pm) or Ti^{2+} (86 pm) ions and this can give rise to an increase in the lattice constants owing to the fact that their ionic radii are higher than that of Ti^{4+} [11].

The strain of the *c*-axis (ε_{zz}) can be determined by the formula [12]:

$$\varepsilon_{zz} = \frac{c - c_0}{c_0} \times 100\%. \quad (3)$$

The strain values of all films are negative, which indicates compressive strains [13]. The compressive

Table 2. Structural properties of undoped and Ti doped ZnO thin films

Sample	Strain ε_{zz} (%)	Grain size D (nm)	Dislocation density δ (lines m^{-2})	Lattice constants	
				a (nm)	c (nm)
ZO	-1.394	34.46	8.42×10^{14}	0.32044	0.51340
TZO-1	-1.452	26.06	1.47×10^{15}	0.32041	0.51310
TZO-2	-1.321	24.75	1.63×10^{15}	0.32119	0.51378
TZO-3	-1.245	23.16	1.86×10^{15}	0.32113	0.51418
TZO-4	-1.198	22.53	1.97×10^{15}	0.32168	0.51442
TZO-5	-1.195	18.45	2.94×10^{15}	0.32324	0.51444

strain value of -1.394 for undoped ZnO firstly rises to the value of -1.452 for TZO-1 sample and then it continuously decreases to the values of -1.321 , -1.244 , -1.198 , and -1.194 for TZO-2, TZO-3, TZO-4, and TZO-5 samples.

The grain size and dislocation density values of films are calculated by Eqs. (4) and (5) [14]:

$$D = \frac{0.9\lambda}{(\beta \cos \theta)}, \quad (4)$$

$$\delta = \frac{1}{D^2}, \quad (5)$$

where D is grain size, δ is dislocation density, λ is an X-ray wavelength of 0.15418 nm, β is full width at half of the peak maximum (FWHM), and θ is Bragg's angle. The calculated grain size and dislocation density values are given in Table 2, and their variation with Ti doping is shown in Fig. 2. The grain size and dislocation density values are found to be 34.46 nm: 8.42×10^{14} lines m^{-2} , 26.06 nm: 1.47×10^{15} lines m^{-2} , 24.75 nm: 1.63×10^{15} lines m^{-2} , 23.16 nm: 1.86×10^{15} lines m^{-2} , 22.53 nm: 1.97×10^{15} lines m^{-2} and 18.45 nm: 2.94×10^{15} lines m^{-2} for ZO, TZO-1, TZO-2, TZO-3, TZO-4 and TZO-5 samples, respectively. The dislocation density can give information about crystallinity of a crystal, and it can be said that there is a decreasing crystallinity in the films with increasing Ti doping. The decreasing crystallinity may be resulted from probably improper lattice position of Ti atoms in ZnO structure. Decreasing crystallinity with Ti doping was also observed in the literature [15].

3.2. Morphological properties

Titanium doping effect on the morphological properties of ZnO thin films is determined by SEM micrographs. The SEM images (Fig. 3) show that all films are composed of nanoparticles and the surface morphology changes with Ti doping. The well-defined grains of the undoped sample are different from a forming nano-network structure with Ti doping. This nano-network structure is formed by collecting the

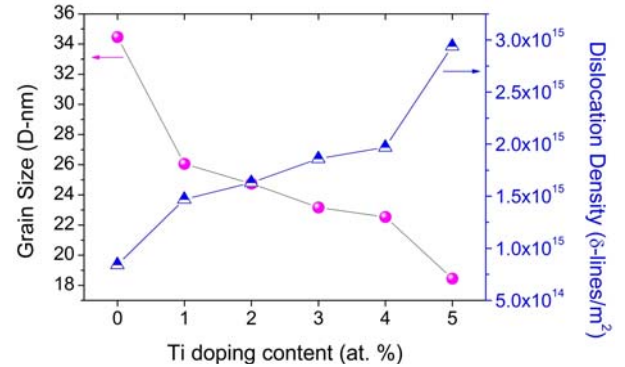


Fig. 2. The variation of grain size and dislocation density values of ZnO with Ti doping.

smaller grains together as soon as Ti is inserted to ZnO. The network line thickness increases with the increasing Ti content. Similar nano-network structure was also observed by Keskenler et al. [16]. Observations from SEM micrographs suggest that Ti dopants in the growth process are very active [17] owing to changing film morphology.

3.3. Optical properties

Optical characterization of undoped and Ti doped films is made with UV/VIS spectrophotometer. Transmittance spectra of the films (Fig. 4) show that the transmittance of films ranges from 65 to 95 % over the visible wavelength region. The transmittance of undoped sample firstly increases with 1 at.% Ti doping and then it continuously decreases with the increasing Ti content. For ultraviolet region, the transmittance of undoped ZnO changes to shorter wavelengths with 1 at.% Ti content (blue shift), then it changes to longer wavelengths with higher Ti level. To identify the absorption band edge of the films, the first derivative of the optical transmittance can be calculated. The curves of $dT/d\lambda$ vs. $h\nu$ have been drawn and represented in Fig. 5. According to other studies [18, 19], maximum peak values of the curves are related to the optical band gap energy and they shift to longer

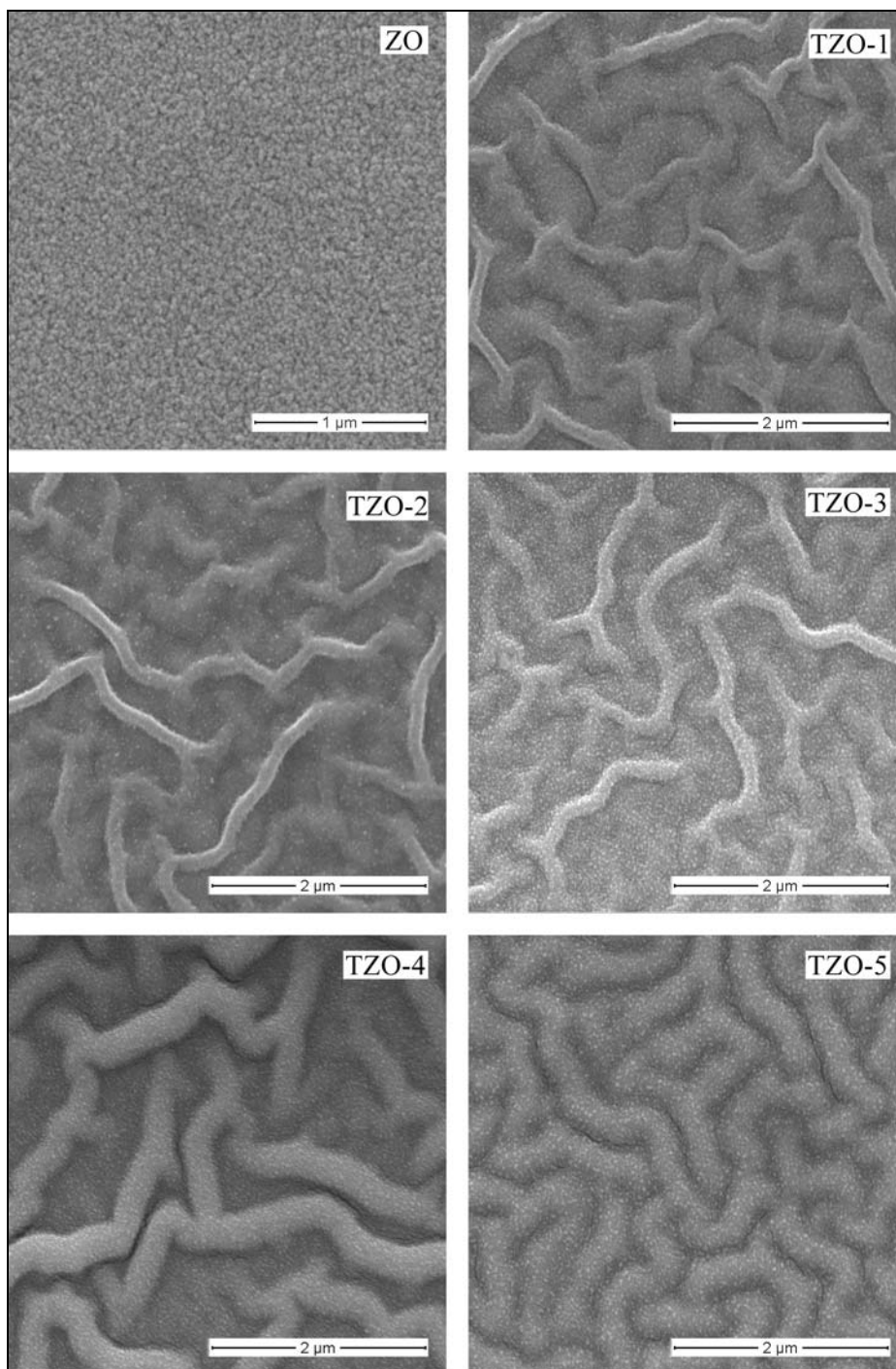


Fig. 3. SEM images of undoped and Ti doped ZnO thin films.

wavelengths with increasing Ti contents. This case can be clearly seen in Fig. 5. From Fig. 6, the maximum peak position is found to be 376, 375, 376, 379, 380 and 382 nm for ZO, TZO-1, TZO-2, TZO-3, TZO-4 and TZO-5 samples, respectively. E_g values obtained from $dT/d\lambda$ curves are seen in Table 3. Additionally, the optical band gap values have also been determined by inflexion point method [20, 21]. To calculate the optical band gap values in this method, following

formula can be used:

$$E_g = \frac{1241.5}{\lambda_c}, \quad (6)$$

where λ_c is the critical wavelength described as the inflexion point of the UV absorption edge. In this method, the location of the λ_c is important. For this purpose, the second derivative of the optical transmission should be calculated (Fig. 6). Optical band gap

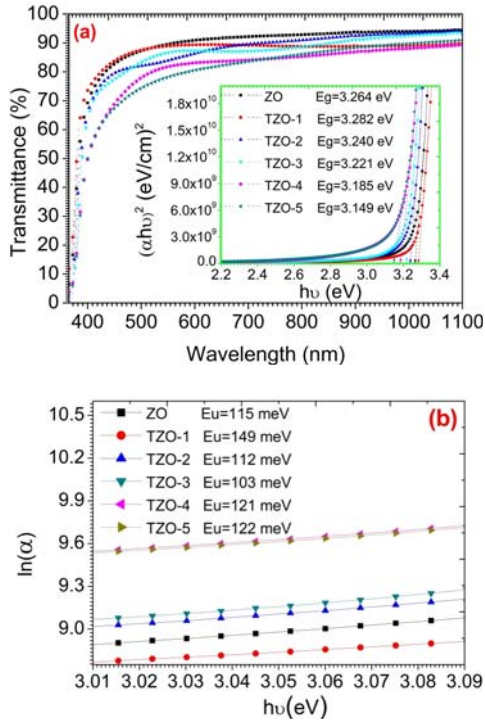


Fig. 4. (a) Optical transmittance (inset figure is $(\alpha h\nu)^2$ vs. $h\nu$ graph), (b) $\ln(\alpha)$ vs. $h\nu$ graph of undoped and Ti doped ZnO thin films.

values that are obtained by an inflexion method are represented in Table 3. Besides, the optical band gap can be calculated more accurately. For this purpose $(\alpha h\nu)^2$ vs. $(h\nu)$ plot has been drawn. To make this, initially the absorption coefficient (α) is calculated by following relation [22]:

$$\alpha = \ln(1/T)/d, \quad (7)$$

then optical band gap values are obtained by equation

$$\alpha h\nu = A(h\nu - E_g)^{1/2}. \quad (8)$$

In Eqs. (7) and (8), T is a transmittance, d is the film thickness, $h\nu$ is photon energy, A is constant. The band gap (E_g) values are determined by drawing $(\alpha h\nu)^2$ vs. $(h\nu)$ (the inset graph in Fig. 4a). The identified band gap values of the films are given in Table 3, and their variation with Ti doping is shown in Fig. 7. The band gap value of undoped sample increases from 3.264 to 3.282 eV with 1 at.% Ti content, then it decreases with further Ti doping to the values of 3.240, 3.221, 3.185 and 3.149 eV for TZO-2, TZO-3, TZO-4 and TZO-5, respectively. The increasing band gap with Ti doping was also found in some studies [8, 23].

For semiconductors, fundamental absorption near the energy band gap increases exponentially, and the

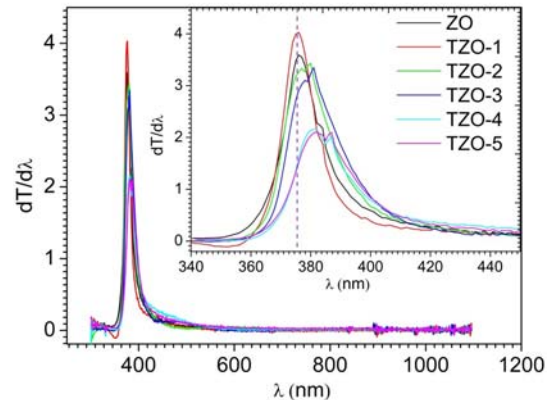


Fig. 5. Curves of $dT/d\lambda$ vs. wavelength of Ti doped ZnO thin films.

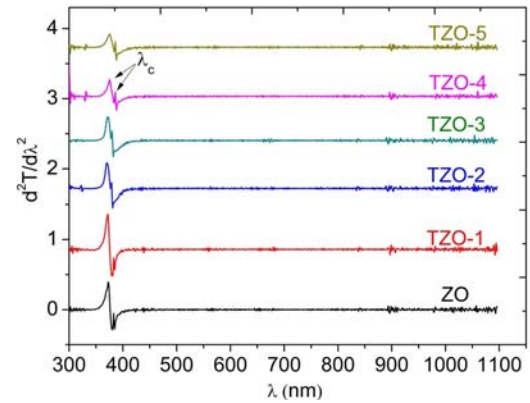


Fig. 6. The plot of $d^2T/d\lambda^2$ vs. wavelength of Ti doped ZnO thin films.

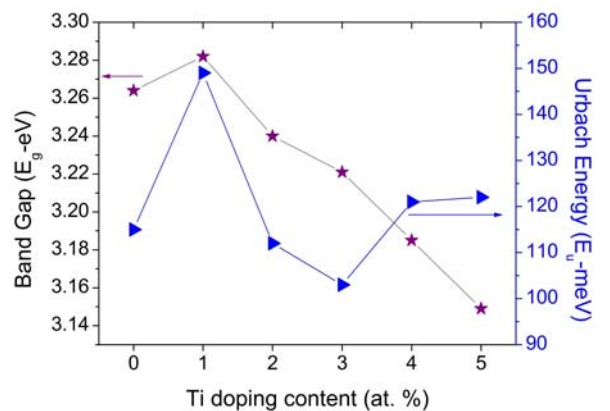


Fig. 7. The variation of optical band gap and Urbach energy values of undoped ZnO with Ti doping.

absorption edge is called the Urbach tail [24]. Urbach energy (E_u) indicates the width of the localized states in the band gap. It may be supposed as a parameter

Table 3. Optical parameters of undoped and Ti doped ZnO thin films

Sample	Transmittance values (%)			λ_c (nm)	Function			E_u (meV)	$\sigma (\times 10^{-1})$
	at 450 nm	at 650 nm	at 850 nm		$(\alpha h\nu)^2$ E_g (eV)	$dT/d\lambda$ E_g (eV)	$d^2T/d\lambda^2$ E_g (eV)		
ZO	82.79	91.67	93.27	374	3.264	3.299	3.319	115	2.24
TZO-1	83.81	89.41	88.79	372	3.282	3.308	3.337	149	1.73
TZO-2	79.48	88.33	91.77	372	3.240	3.299	3.337	112	2.31
TZO-3	77.42	87.03	89.82	375	3.221	3.273	3.310	103	2.51
TZO-4	68.99	83.64	86.09	376	3.185	3.265	3.301	121	2.14
TZO-5	67.47	82.15	87.24	377	3.149	3.247	3.293	122	2.12

containing the effects of all possible defects, and it depends on the degree of structural disorders. The Urbach energies are determined by following equation [25]:

$$\alpha = \alpha_0 \exp\left(\frac{h\nu - E_0}{E_u}\right), \quad (9)$$

where E_0 and α_0 are constants. The E_u is the Urbach energy that is designating the steepness of Urbach tail. If it takes the logarithm of Eq. (9), the following equation can be written:

$$\ln \alpha = E \frac{1}{E_u} \left(\ln(\alpha_0) + \frac{E_0}{E_u} \right), \quad (10)$$

where E_u is equal to the absorption edge energy width and inverse to the absorption edge slope value $E_u^{-1} = \Delta(\ln \alpha)/\Delta(h\nu)$. E_u energies of the films are calculated from the slope of the $\ln \alpha$ vs. photon energy ($h\nu$) plot (Fig. 4b). The variations of calculated E_u values with Ti doping are given in Fig. 7. The E_u value of 115 meV of the undoped film increases to the value of 149 meV for TZO-1 sample and then it starts to decrease to the values of 112 and 103 meV for TZO-2 and TZO-3 samples. When the Ti doping ratio is increased over 3 at.% content, E_u values increase to 121 and 122 meV in TZO-4 and TZO-5 samples.

The steepness parameter (σ) of films is calculated by the following relation:

$$\sigma = k_B T / E_u, \quad (11)$$

where k_B is Boltzmann constant, T is temperature at 300 K. The σ value of undoped ZnO decreases from 2.24×10^{-1} to 1.73×10^{-1} for TZO-1, and then it increases to the values of 2.31×10^{-1} , 2.51×10^{-1} in TZO-2, TZO-3 samples. Finally, it starts to decrease to the values of 2.14×10^{-1} and 2.12×10^{-1} in TZO-4 and TZO-5 films. There are many determinants affecting the optical band gap of ZnO such as non-stoichiometry, grain size, disorders, lattice parameters and carrier concentration [26, 27].

According to E_u values, E_g value of undoped ZnO would decrease with 1 at.% Ti doping due to structural disorders and transitions from band to tail and tail to tail [28]. The increasing E_g values with 1 at.% Ti doping are probably resulting from the Moss-Burstein (MB) effect [29]. In the MB effect, Zn^{2+} ions are replaced by Ti^{4+} ions, and this introduces an increase in the carrier density. Thus, Fermi level lifts into the conduction band, and optical band gap rises. The decreasing optical band gap with the increasing Ti content can be resulted from the increasing structural disorders, lattice imperfections and decreasing crystallinity, which can be seen from XRD results, and transitions from band to tail and tail to tail.

4. Conclusions

Fabrication and investigation studies on Ti doped ZnO thin films by sol-gel spin coating technique were made as a function of Ti doping ratio. The XRD studies showed that Ti doped ZnO thin films with polycrystalline structure had (002) preferential orientation, and the film crystallinity decreased with Ti doping. From SEM micrographs, it was seen that the nanoparticle structure of undoped ZnO changed to nano-network structure when Ti atoms were inserted into the ZnO structure. The optical transmittance and band gap values of undoped ZnO initially increased with 1 at.% Ti content, but then further Ti doping caused a decrease in optical transmittance and band gap values. Urbach energy and steepness parameter values were also studied, and it was found that they depended on Ti doping content. The results obtained have proved that Ti doped ZnO films can be successfully grown by a sol-gel spin coating method, and these films can be useful for many optoelectronic device applications.

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